

MATH 161 EXAM III NAME: \_\_\_\_\_

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[ Run: 04/17/2013 at 14:5 Seed: 1876. Order of Checkable Items: Random. ]

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**Response Grid** (Check the appropriate boxes thus:  )

Question	a	b	c	d	e
1					
2					
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**III-1.** Let the function  $f$  be specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{-x^2 - 9}{(x - 1)^2}$$

find the approximate local input-output rule of  $f$  that gives the concavity-sign near  $\infty$ .

- a.  $x \xrightarrow{f_\infty} f_\infty(x) = -1 + x^{-1} + [\dots]$
- b.  $x \xrightarrow{f_\infty} f_\infty(x) = -1 - 2x^{-1} + [\dots]$
- c.  $x \xrightarrow{f_\infty} f_\infty(x) = -x^2 + [\dots]$
- d.  $x \xrightarrow{f_\infty} f_\infty(x) = -1 + x^2 + [\dots]$
- e. None of the preceding

**III-2.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{(x + 1)^2}{x - 2}$$

how many Height-sign change inputs does  $f$  have?

- a. None      b. One      c. Two      d. Three
- e. None of the preceding

**III-3.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{(x - 1)^2}{x^3 - 8}$$

how many Concavity-sign change inputs does  $f$  have?

- a. None      b. One      c. Two      d. Three
- e. None of the preceding

**III-4.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x - 1}{x^3 - 8}$$

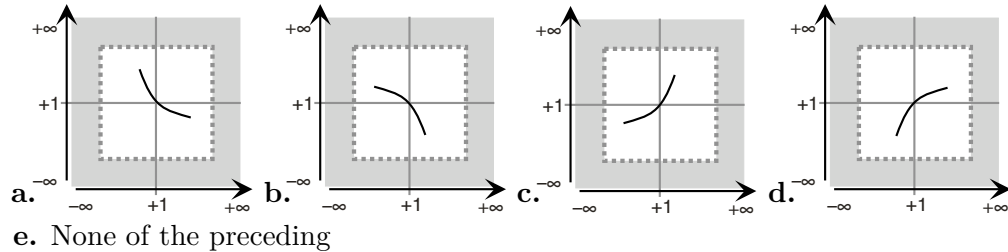
find the approximate input-output local rule for graph near  $+2$

- a.  $h \xrightarrow{f_{+2}} f_{+2}(h) = +12h^{-1} + [\dots]$
- b.  $h \xrightarrow{f_{+2}} f_{+2}(h) = +12h + [\dots]$
- c.  $h \xrightarrow{f_{+2}} f_{+2}(h) = +\frac{1}{12}h^{-1} + [\dots]$
- d.  $h \xrightarrow{f_{+2}} f_{+2}(h) = -12h + [\dots]$
- e. None of the preceding

**III-5.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x^3 - 4}{x^2 - 4}$$

find the local graph of  $f$  near  $+1$ .



**III-6.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x^2 + x + 1}{(x - 2)^2}$$

find the Slope sign of  $f$  near  $+2$ .

- a. ( $\swarrow$ ,  $\swarrow$ )    b. ( $\swarrow$ ,  $\searrow$ )    c. ( $\searrow$ ,  $\swarrow$ )    d. ( $\searrow$ ,  $\searrow$ )  
 e. None of the preceding

**III-7.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x - 1}{x^3 - 1}$$

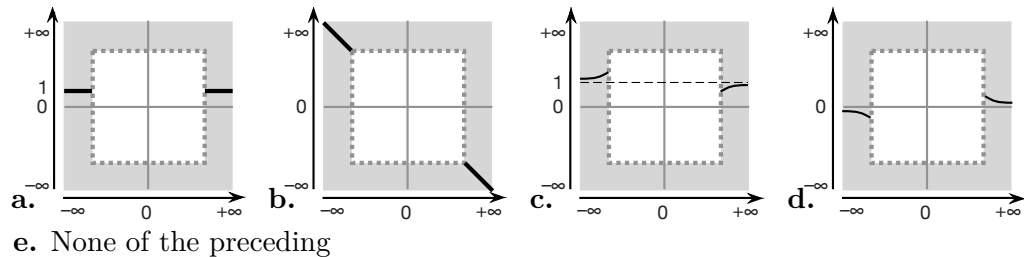
find the approximate local input-output rule that gives the local graph near 0.

- a.  $h \xrightarrow{f_0} f_0(h) = +1 + h + h^2 + [\dots]$   
 b.  $h \xrightarrow{f_0} f_0(h) = +1 - h + h^2 + [\dots]$   
 c.  $h \xrightarrow{f_0} f_0(h) = +1 - h + h^3 + [\dots]$   
 d.  $h \xrightarrow{f_0} f_0(h) = +1 + h + h^3 + [\dots]$   
 e. None of the preceding

**III-8.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x^2 + 1}{(x - 1)^2}$$

find the local graph of  $f$  near  $\infty$ .



**III-9.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x^2 - 9}{(x - 3)^2}$$

find the 0-height inputs of  $f$ .

- a.  $-3, +1$       b.  $-3$       c.  $+3$       d.  $-3, +1, +3$   
 e. None of the preceding

**III-10.** Let  $f$  be the function specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{+3x^2 + 4x - 4}{-12x^5 + 4x^2 + 1}$$

find the Height sign of  $f$  near  $\infty$ .

- a.  $(+, +)$       b.  $(+, -)$       c.  $(-, +)$       d.  $(-, -)$   
 e. None of the preceding

**III-11.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x^2 - 1}{(x - 3)^2}$$

find the Concavity-sign of  $f$  near  $+3$ .

- a.  $(\cup, \cup)$       b.  $(\cup, \cap)$       c.  $(\cap, \cup)$       d.  $(\cap, \cap)$   
 e. None of the preceding

**III-12.** Let  $f$  be the function specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{(x^2 - 3)^2}{x^8 - 16}$$

find Slope sign of  $f$  near  $\infty$ .

- a.  $(\swarrow, \swarrow)$       b.  $(\swarrow, \searrow)$       c.  $(\searrow, \swarrow)$       d.  $(\searrow, \searrow)$   
 e. None of the preceding

**III-13.** Let  $f$  be the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x^4 - 16}{x^2 - 9}$$

what is the answer to the ESSENTIAL QUESTION?

- a. No  $\infty$ -height bounded input.  
 b. Two  $\infty$ -height bounded inputs:  $-2$  and  $+2$ .  
 c. Two  $\infty$ -height bounded inputs:  $-3$  and  $+3$ .  
 d. Four  $\infty$ -height bounded inputs:  $-2$ ,  $+2$  and  $-3$ ,  $+3$ .  
 e. None of the preceding

**III-14.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x^2 - 9}{(x - 3)^2}$$

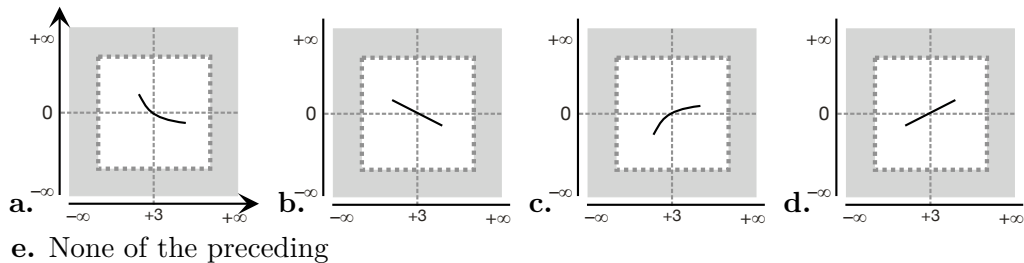
find the  $\infty$ -height inputs of  $f$ .

- a.  $-3, +1$     b.  $-3$     c.  $+3$     d.  $-3, +1, +3$   
 e. None of the preceding

**III-15.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x^2 - 9}{x^2 + 9}$$

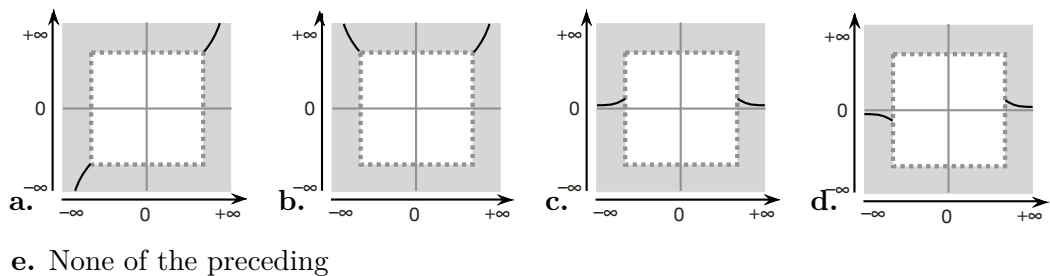
find the local graph of  $f$  near  $+3$ .



**III-16.** Let the function  $f$  be specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x - 3}{x^4 - 1}$$

Find the local graph of  $f$  near  $\infty$ .



**III-17.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x^2 + 9}{(x - 3)^2}$$

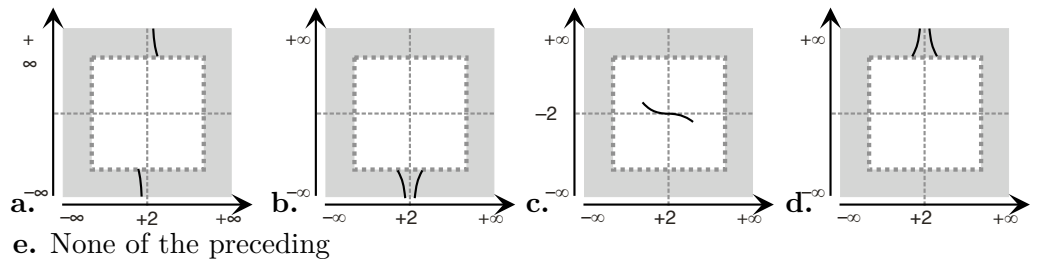
find the Height sign of  $f$  near  $+3$ .

- a.  $(+, +)$     b.  $(+, -)$     c.  $(-, +)$     d.  $(-, -)$   
 e. None of the preceding

**III-18.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{(x-2)(x+3)}{x^2-4x+4}$$

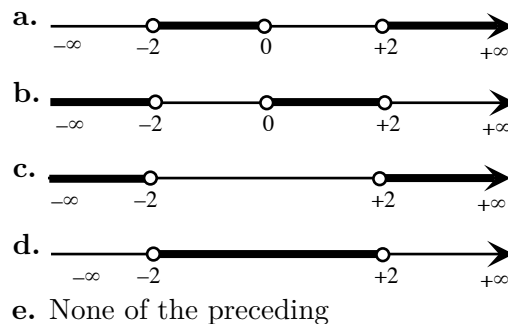
find the local graph of  $f$  near  $+2$ .



**III-19.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x^2-4}{x^2}$$

for which input(s), if any, is the output of  $f$  positive?



**III-20.** Given the function  $f$  specified by the global input-output rule

$$x \xrightarrow{f} f(x) = \frac{x^2-1}{x^3-8}$$

find the approximate local input-output rule that gives the local graph near  $+1$ .

- a.  $h \xrightarrow{f_{+1}} f_{+1}(h) = -\frac{2}{8}h^{-1} + [\dots]$   
 b.  $h \xrightarrow{f_{+1}} f_{+1}(h) = -8 + 19h - 27h^2 + [\dots]$   
 c.  $h \xrightarrow{f_{+1}} f_{+1}(h) = +\frac{1}{4}h^{-1} + [\dots]$   
 d.  $h \xrightarrow{f_{+1}} f_{+1}(h) = -\frac{2}{8}h^{+1} - \frac{14}{8^2}h^{+2} + [\dots]$   
 e. None of the preceding